

Homk 2 EECE622
Winter 2012

(I) Prove the following identities (using truth tables).

$$A \text{ AND } 0 = 0$$

$$A + 1 = 1$$

$$A + (A \text{ AND } B) = A$$

$$A + (\sim A) \text{ AND } B = A + B$$

\sim is the NOT OPERATION

(II) Using the following table

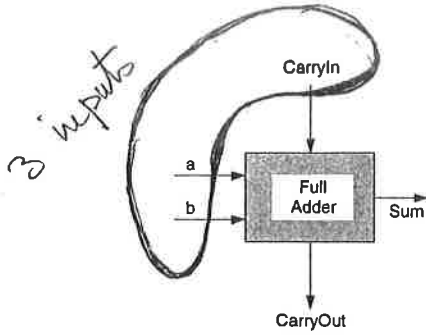
AB	f0	f1	f2	f3	f4	f5	f6	f7	f8	f9	fa	fb	fc	fd	fe	ff
00	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
01	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
10	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
11	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1

Show $f_9 = (\sim A)(\sim B) + AB$

$$f_6 = A(\sim B) + (\sim A)B$$

$$f_2 = A(\sim B)$$

III) Using the truth table of the full adder below



a	b	CarryIn	Sum	CarryOut
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Show

$$Sum = \bar{a}\bar{b}CarryIn + \bar{a}b\overline{CarryIn} + a\bar{b}\overline{CarryIn} + abCarryIn$$

$$CarryOut = \bar{a}bCarryIn + a\bar{b}CarryIn + ab\overline{CarryIn} + abCarryIn$$

By manipulation of the last Boolean expression, show that

$$CarryOut = ab + aCarryIn + bCarryIn.$$

(IV) Show how to use the QCA described in class to implement an AND gate starting with the majority voting logic architecture discussed in class.